

$$\sum_{n=1}^{\infty} \sin(\pi \sqrt{n^2 + k^2})$$

$$\sqrt{n^2 + k^2} - n = \frac{k^2}{\sqrt{n^2 + k^2} + n} \rightarrow 0$$

for  $n \rightarrow +\infty$

$$\sin(\pi \sqrt{n^2 + k^2}) - \sin(n\pi)$$

$$(-1)^n \sin(\pi (\sqrt{n^2 + k^2} - n)) = \frac{1}{(-1)^n} \sin(\pi \sqrt{n^2 + k^2})$$

$$\sum_{n=1}^{\infty} \frac{k^2}{\sqrt{n^2 + k^2} + n} = +\infty$$